

Marking Scheme
Strictly Confidential
(For Internal and Restricted use only)
Senior Secondary Supplementary School Examination, 2026 (XII)
SUBJECT NAME: MATHEMATICS (041) (Q.P. CODE /Set No: 65/7/2)

General Instructions: -

1	You are aware that evaluation is the most important process in the actual and correct assessment of the candidates. A small mistake in evaluation may lead to serious problems which may affect the future of the candidates, education system and teaching profession. To avoid mistakes, it is requested that before starting evaluation, you must read and understand the spot evaluation guidelines carefully.
2	“Evaluation policy is a confidential policy as it is related to the confidentiality of the examinations conducted, evaluation done and several other aspects. Its leakage to public in any manner could lead to derailment of the examination system and affect the life and future of millions of candidates. Sharing this policy/document to anyone, publishing in any magazine and printing in Newspaper/Website, etc. may invite action under various rules of the Board and IPC.”
3	Evaluation is to be done as per instructions provided in the Marking Scheme. It should not be done according to one’s own interpretation or any other consideration. Marking Scheme should be strictly adhered to and religiously followed. However, while evaluating, answers which are based on latest information or knowledge and/or are innovative, they may be assessed for their correctness otherwise and due marks be awarded to them. In Class-XII, while evaluating two competency-based questions, please try to understand given answer and even if reply is not from marking scheme but correct competency is enumerated by the candidate, due marks should be awarded.
4	The Marking scheme carries only suggested value points for the answers. These are in the nature of Guidelines only and do not constitute the complete answer. The students can have their own expression and if the expression is correct, the due marks should be awarded accordingly.
5	The Head-Examiner must go through the first five answer books evaluated by each evaluator on the first day, to ensure that evaluation has been carried out as per the instructions given in the Marking Scheme. If there is any variation, the same should be zero after deliberation and discussion. The remaining answer books meant for evaluation shall be given only after ensuring that there is no significant variation in the marking of individual evaluators.
6	Evaluators will mark (✓) wherever answer is correct. For wrong answer CROSS ‘X’ be marked. Evaluators will not put right (✓) while evaluating which gives an impression that answer is correct and no marks are awarded. This is most common mistake which evaluators are committing.
7	If a question has parts, please award marks on the right-hand side for each part. Marks awarded for different parts of the question should then be totaled up and written in the left-hand margin and encircled. This may be followed strictly.
8	If a question does not have any parts, marks must be awarded in the left-hand margin and encircled. This may also be followed strictly.
9	If a student has attempted an extra question, answer of the question deserving more marks should be retained and the other answer scored out with a note “Extra Question” .
10	No marks to be deducted for the cumulative effect of an error. It should be penalized only once.
11	A full scale of marks 0 to 80 has to be used. Please do not hesitate to award full marks if the answer deserves it.

12	Every examiner has to necessarily do evaluation work for full working hours i.e., 8 hours every day and evaluate 20 answer books per day in main subjects and 25 answer books per day in other subjects (Details are given in Spot Guidelines). This is in view of the reduced syllabus and number of questions in question paper.
13	Ensure that you do not make the following common types of errors committed by the Examiner in the past :- ● Leaving answer or part thereof unassessed in an answer book. ● Giving more marks for an answer than assigned to it. ● Wrong totaling of marks awarded on an answer. ● Wrong transfer of marks from the inside pages of the answer book to the title page. ● Wrong question wise totaling on the title page. ● Wrong totaling of marks of the two columns on the title page. ● Wrong grand total. ● Marks in words and figures not tallying/not same. ● Wrong transfer of marks from the answer book to online award list. ● Answers marked as correct, but marks not awarded. (Ensure that the right tick mark is correctly and clearly indicated. It should merely be a line. Same is with the X for incorrect answer.) ● Half or a part of answer marked correct and the rest as wrong, but no marks awarded.
14	While evaluating the answer books if the answer is found to be totally incorrect, it should be marked as cross (X) and awarded zero (0) Marks.
15	Any unassessed portion, non-carrying over of marks to the title page, or totaling error detected by the candidate shall damage the prestige of all the personnel engaged in the evaluation work as also of the Board. Hence, in order to uphold the prestige of all concerned, it is again reiterated that the instructions be followed meticulously and judiciously.
16	The Examiners should acquaint themselves with the guidelines given in the “ Guidelines for Spot Evaluation ” before starting the actual evaluation.
17	Every Examiner shall also ensure that all the answers are evaluated, marks carried over to the title page, correctly totaled and written in figures and words.
18	The candidates are entitled to obtain photocopy of the Answer Book on request on payment of the prescribed processing fee. All Examiners/Additional Head Examiners/Head Examiners are once again reminded that they must ensure that evaluation is carried out strictly as per value points for each answer as given in the Marking Scheme.

MARKING SCHEME
MATHEMATICS CLASS XII (Subject Code-041)
(PAPER CODE: 65/7/2)

Q. No.	EXPECTED OUTCOMES/VALUE POINTS	Steps	Marks
	SECTION A		
	Q. Number 1 to 20 are multiple choice questions of 1 mark each.		
1.	For $f(x) = - x + 1 + 5$, which of the following statements is true ? (A) Max $f(x) = 0$ at $x = 4$. (B) Max $f(x) = 5$ at $x = -1$. (C) Max $f(x) = 4$ at $x = 0$. (D) $f(x)$ has no maximum value.		
Ans.	(B) Max $f(x) = 5$ at $x = -1$		1
2.	If $f(x) = \begin{cases} \frac{ x }{x}, & x \neq 0 \\ 0, & x = 0 \end{cases}$, then which of the following statements is not correct ? (A) f is continuous for every $x < 0$. (B) f is continuous for every $x \in \mathbb{R}$. (C) f is continuous for every $x > 0$. (D) f is continuous for each point except $x = 0$.		
Ans.	(B) f is continuous for every $x \in \mathbb{R}$		1
3.	The value of $\cos^{-1}\left[\cos \frac{7\pi}{6}\right]$ is : (A) $\frac{7\pi}{6}$ (B) $\frac{5\pi}{6}$ (C) $\frac{\pi}{3}$ (D) $\frac{\pi}{6}$		
Ans	(B) $\frac{5\pi}{6}$		1
4.	If $\begin{vmatrix} 3x & x+2 \\ 3(x-1) & x-2 \end{vmatrix} = \begin{vmatrix} 1 & 5 \\ 3 & 3 \end{vmatrix}$, then the value of x is : (A) 2 (B) $\frac{1}{3}$ (C) 5 (D) 3		

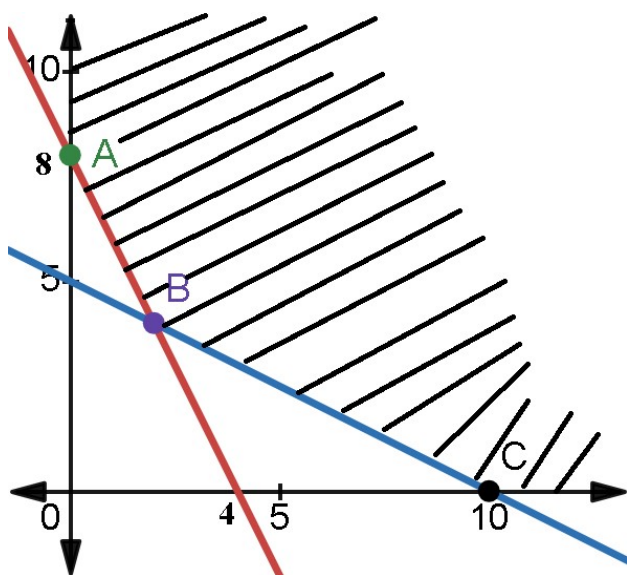
Ans.	(A) 2		1
5.	If A is a square matrix, then which of the following is not true ? (A) $A + A'$ is a symmetric matrix (B) AA' and $A'A$ are symmetric matrices (C) $A + A'$ is a skew symmetric matrix (D) $A - A'$ is a skew symmetric matrix		
Ans.	(C) $A + A'$ is a skew symmetric matrix		1
6.	If $A = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$ satisfies $A' + A = I$, then the value of θ is : (A) $\frac{\pi}{6}$ (B) $\frac{\pi}{3}$ (C) $\frac{2\pi}{3}$ (D) $\frac{5\pi}{6}$		
Ans.	(B) $\frac{\pi}{3}$		1
7.	$[\tan^{-1} \sqrt{3} - \sec^{-1} (-2)]$ is equal to : (A) π (B) $-\frac{\pi}{3}$ (C) $\frac{\pi}{3}$ (D) $\frac{2\pi}{3}$		
Ans.	(B) $-\frac{\pi}{3}$		1
8.	Differential of $\cos^{-1}(e^x)$ with respect to x is : (A) $\frac{e^x}{\sqrt{1-e^{2x}}}$ (B) $\frac{-e^x}{\sqrt{1+e^x}}$ (C) $\frac{-e^x}{\sqrt{1-e^{2x}}}$ (D) $\frac{e^x}{\sqrt{1+e^{2x}}}$		
Ans.	(C) $\frac{-e^x}{\sqrt{1-e^{2x}}}$		1

9.	If $\int_0^1 (9x^2 - 4x - 2k) dx = 0$, then the value of 'k' is : (A) 1 (B) 0 (C) $\frac{1}{2}$ (D) $-\frac{1}{2}$		
Ans.	(C) $\frac{1}{2}$		1
10.	If A and B are square matrices of order 3 such that $A = 4$ and $B = 7$, then $2AB$ is : (A) 112 (B) 56 (C) 28 (D) 224		
Ans.	(D) 224		1
11.	If the rate of change of the area of a circle is equal to the rate of change of its diameter, then its radius is : (A) 2π units (B) π units (C) $\frac{\pi}{2}$ units (D) $\frac{1}{\pi}$ units		
Ans.	(D) $\frac{1}{\pi}$ units		1
12.	If vectors $\vec{a} = 3\hat{i} - 2\hat{j} + 4\hat{k}$ and $\vec{b} = \lambda\hat{i} + \hat{j}$ are perpendicular to each other, then the value of λ is : (A) 3 (B) -3 (C) $\frac{2}{3}$ (D) $-\frac{2}{3}$		
Ans.	(C) $\frac{2}{3}$		1
13.	$\int [\sin(\log x) + \cos(\log x)] dx$ is equal to : (A) $-\cos(\log x) + C$ (B) $\frac{1}{\cos x} + \frac{1}{\sin x} + C$ (C) $\sin(\log x) + C$ (D) $x \sin(\log x) + C$		
Ans.	(D) $x \sin(\log x) + C$		1

14.	If $y = \sqrt{y + \cos x}$, then $\frac{dy}{dx}$ is equal to : (A) $\frac{1}{2\sqrt{y + \cos x}}$ (B) $\frac{\cos x}{2y - 1}$ (C) $\frac{-\sin x}{2\sqrt{y + \cos x}}$ (D) $\frac{\sin x}{1 - 2y}$		
Ans.	(D) $\frac{\sin x}{1 - 2y}$		1
15.	If $A = \begin{bmatrix} 1 & -2 & 3 \\ 3 & 2 & -1 \end{bmatrix}$, $B = \begin{bmatrix} 2 & 3 \\ -1 & 2 \\ 4 & -5 \end{bmatrix}$ and $C = [C_{ij}] = AB$, then C_{12} is : (A) 22 (B) -16 (C) 4 (D) 0		
Ans.	(B) -16		1
16.	If two events A and B are independent, then which of the following statements is not correct ? (A) $\bar{A}$ and B are independent. (B) Being independent does not indicate that they are mutually exclusive. (C) $P(\bar{A} \cap \bar{B}) = [1 - P(\bar{A})] [1 - P(\bar{B})]$. (D) $P(\bar{A} \cap \bar{B}) = [1 - P(A)] [1 - P(B)]$.		
Ans.	(C) $P(\bar{A} \cap \bar{B}) = [1 - P(\bar{A})] [1 - P(\bar{B})]$.		1
17.	If $\int_0^4 \frac{1}{x + \sqrt{x}} dx = k \log 3$, then the value of k is : (A) 4 (B) -2 (C) -4 (D) 2		
Ans.	(D) 2		1

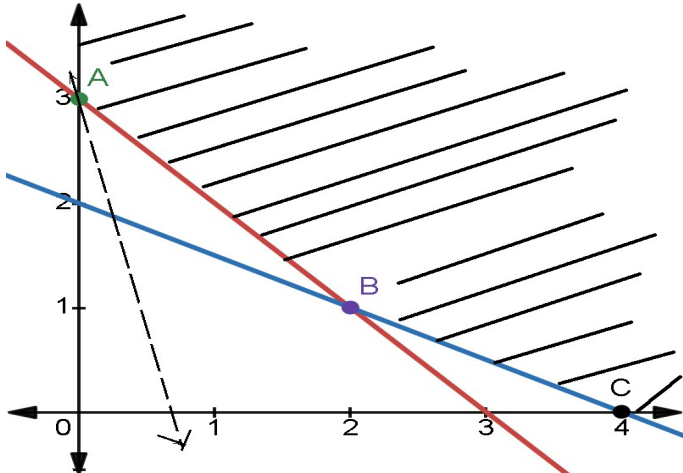
18.	For events A and B, if $P(B) = \frac{3}{5}$, $P(A/B) = \frac{1}{2}$ and $P(A \cup B) = \frac{4}{5}$, then P(A) is : (A) $\frac{1}{2}$ (B) $\frac{3}{5}$ (C) $\frac{1}{5}$ (D) $\frac{3}{10}$		
Ans.	(A) $\frac{1}{2}$		1
19.	<i>Assertion (A) :</i> Let R be a relation on set A of all books in a school library given by $R = \{(x, y) : x, y \in A, x \text{ and } y \text{ have the same number of pages}\}$ and S is a relation on set A from the same library such that $S = \{(p, q) : p \text{ and } q \text{ are Mathematics books}\}$. Also, $R \cap S \neq \phi$. Then, $R \cap S$ is an equivalence relation. <i>Reason (R) :</i> The intersection of two equivalence relations on a set is an equivalence relation on the set.		
Ans.	(D) Assertion (A) is false, but Reason (R) is true.		1
20.	<i>Assertion (A) :</i> Points A(6, – 7, 0), B(16, –19, – 4) and C(1, – 1, 2) are collinear. <i>Reason (R) :</i> Three points A, B and C are collinear, when point C is the mid-point of line segment joining points A and B.		
Ans.	(B) Both Assertion (A) and Reason (R) are true, but Reason (R) is not the correct explanation of the Assertion (A).		1
SECTION B			
Q. Numbers 21 to 25 are very short answer questions of 2 marks each.			
21.	Solve the given matrix equation for x, given $x > 0$: $x \begin{bmatrix} 2x & 2 \\ 3 & x \end{bmatrix} + 2 \begin{bmatrix} 8 & 5x \\ 4 & 0 \end{bmatrix} = 2 \begin{bmatrix} x^2 + 8 & 24 \\ 10 & 8 \end{bmatrix}$		2
Sol.	The given equation can be written as, $\begin{bmatrix} 2x^2 + 16 & 12x \\ 3x + 8 & x^2 \end{bmatrix} = \begin{bmatrix} 2x^2 + 16 & 48 \\ 20 & 16 \end{bmatrix}$ On comparing, we get $12x = 48 \Rightarrow x = 4$ Since, $x = 4$ satisfies $3x + 8 = 20$ and $x^2 = 16$ Thus, $x = 4$	I II III	1 $\frac{1}{2}$ $\frac{1}{2}$

22.	Students are trying to fix thumb pins on a graph sheet on the class notice board. A relation R is defined on the set A of thumb pins as $R = \{(P, Q) : P, Q \in A \text{ and distance between P and Q is less than 3 cm}\}$ Determine if R is an equivalence relation.		
Sol:	Let d(P, Q) denotes distance between any point P and Q For any point P on set A, the distance from P to itself is zero. $d(P, P) = 0 < 3$, $(P, P) \in R$. Therefore, R is reflexive. Let $(P, Q) \in R$, then $d(P, Q) < 3$. As, $d(P, Q) = d(Q, P)$. Thus, $d(Q, P) < 3$, which means $(Q, P) \in R$. Therefore, R is symmetric. Let $(P, Q) \in R$, so $d(P, Q) < 3$ and $(Q, S) \in R$ so $d(Q, S) < 3$, then $(P, S) \notin R$ for example Let P, Q and R be any three different points on the same line such that $d(P, Q) = 2$ cm and $d(Q, R) = 2$ cm so $d(P, R) = 4$ cm > 3 Therefore, R is not transitive. Thus, R is not an equivalence relation. **Note: If a student shows only Transitive part correctly (Without mentioning anything about Reflexive and Symmetric part), then also solution deserve full 2 marks. Alternative example are also acceptable.	I	$\frac{1}{2}$
		II	$\frac{1}{2}$
		III	1
23. (a)	A box contains cards numbered 1 to 22. Two cards are drawn simultaneously without replacement and their numbers are noted. What is the probability that both numbers are even ?		
Sol:	As, box contain 11 even numbers and 11 odd numbers. $P(\text{Both Even numbers}) = \frac{11}{22} \times \frac{10}{21} \text{ or } \frac{{}^{11}C_2}{{}^{22}C_2}$ $\text{Thus, } P(\text{Both Even numbers}) = \frac{5}{21}$	I	$\frac{1}{2}$
		II	1
		III	$\frac{1}{2}$
OR			
23. (b)	If $P(A) = \frac{3}{8}$, $P(B) = \frac{1}{2}$ and $P(A \cap B) = \frac{1}{4}$, find $P(\bar{A} \bar{B})$.		
Sol:	As, $P(A \cup B) = \frac{3+4-2}{8} = \frac{5}{8}$ So, $P(\bar{A} \bar{B}) = \frac{P(\bar{A} \cap \bar{B})}{P(\bar{B})} = \frac{1-P(A \cup B)}{1-P(B)}$	I	1
		II	$\frac{1}{2}$

	Thus, $P(\bar{A} \bar{B}) = \frac{3/8}{1/2} = \frac{3}{4}$	III	$\frac{1}{2}$
24.	For the given Linear Programming Problem, shade the feasible region on the graph and write the coordinates of the corner points. Minimize $Z = 5x + 7y$ subject to constraints $2x + y \geq 8$ $x + 2y \geq 10$ $x, y \geq 0.$		
Sol.	 Corner points are A (0, 8), B (2, 4) and C(10, 0).	I II	1 (For Correct Graph and shading) 1
25. (a)	Determine a and b if $f(x)$ is a continuous function, where $f(x) = \begin{cases} 2, & x \leq 3 \\ ax + b, & 3 < x < 5 \\ 5, & x \geq 5 \end{cases}$		
Sol.	For getting $3a + b = 2$ For getting $5a + b = 5$ Thus, $a = \frac{3}{2}$ and $b = \frac{-5}{2}$	I II III	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2} + \frac{1}{2}$
OR			

25. (b)	If $2y^3 + y = 2x$, then show $\frac{d^2y}{dx^2} = \frac{-48y}{(6y^2 + 1)^3}$.		
Sol.	As, $2y^3 + y = 2x \Rightarrow (6y^2 + 1) \frac{dy}{dx} = 2$ Thus, $\frac{dy}{dx} = \frac{2}{6y^2 + 1}$ On again Differentiating w.r.t. x, we get $\frac{d^2y}{dx^2} = \frac{-24y}{(6y^2 + 1)^2} \times \frac{dy}{dx}$ $\frac{d^2y}{dx^2} = \frac{-24y}{(6y^2 + 1)^2} \times \frac{2}{6y^2 + 1} = \frac{-48y}{(6y^2 + 1)^3}$	I II III IV	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
SECTION C			
Q. Numbers 26 to 31 are short answer questions of 3 marks each.			
26. (a)	Express the matrix $A = \begin{bmatrix} 2 & 4 \\ 5 & 6 \end{bmatrix}$ as the sum of a symmetric matrix and a skew symmetric matrix.		
Sol :	As, $A = \begin{bmatrix} 2 & 4 \\ 5 & 6 \end{bmatrix} \Rightarrow A' = \begin{bmatrix} 2 & 5 \\ 4 & 6 \end{bmatrix}$ So, $A + A' = \begin{bmatrix} 4 & 9 \\ 9 & 12 \end{bmatrix}$ and $A - A' = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$ Thus, $A = \frac{1}{2}(A + A') + \frac{1}{2}(A - A') = \begin{bmatrix} 2 & \frac{9}{2} \\ \frac{9}{2} & 6 \end{bmatrix} + \begin{bmatrix} 0 & \frac{-1}{2} \\ \frac{1}{2} & 0 \end{bmatrix}$	I II III	$\frac{1}{2}$ 1 $1\frac{1}{2}$
OR			
26. (b)	Two lines are represented by equations $5x - 7y - 2 = 0$ and $7x - 5y - 3 = 0$ in the xy-plane. Using matrix method, find their point of intersection.		
Sol :	Given equations can be written in matrix form as $\begin{bmatrix} 5 & -7 \\ 7 & -5 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 2 \\ 3 \end{bmatrix} \Rightarrow AX = B \Rightarrow X = A^{-1}B \quad (A = 24 \neq 0, \therefore A^{-1} \text{ exists})$ A X B Now, $A^{-1} = \frac{1}{24} \begin{bmatrix} -5 & 7 \\ -7 & 5 \end{bmatrix}$ Thus, $X = \frac{1}{24} \begin{bmatrix} -5 & 7 \\ -7 & 5 \end{bmatrix} \begin{bmatrix} 2 \\ 3 \end{bmatrix} = \begin{bmatrix} \frac{11}{24} \\ \frac{1}{24} \end{bmatrix} \Rightarrow x = \frac{11}{24}, y = \frac{1}{24}$	I II III	$\frac{1}{2} + \frac{1}{2}$ 1 1

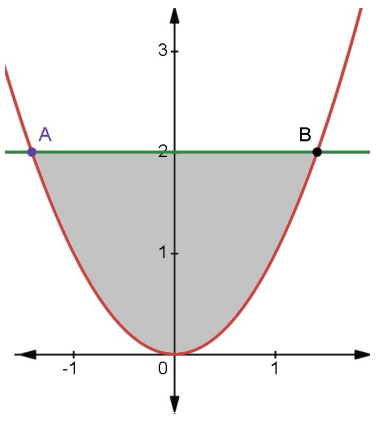
	$\therefore$ The point of intersection of the two lines is $\left(\frac{11}{24}, \frac{1}{24}\right)$.		
27.	If $y = \left\{x + \sqrt{x^2 - a^2}\right\}^n$, then prove that $\frac{dy}{dx} = \frac{ny}{\sqrt{x^2 - a^2}}$.		
Sol.	$\frac{dy}{dx} = n(x + \sqrt{x^2 - a^2})^{n-1} \times \frac{d}{dx}(x + \sqrt{x^2 - a^2})$ $\frac{dy}{dx} = n(x + \sqrt{x^2 - a^2})^{n-1} \times \left(1 + \frac{x}{\sqrt{x^2 - a^2}}\right)$ $\frac{dy}{dx} = \frac{n(x + \sqrt{x^2 - a^2})^n}{\sqrt{x^2 - a^2}} = \frac{ny}{\sqrt{x^2 - a^2}}$	I II III	1 1 1
28.	Find the sum of maximum and minimum values of $f(x) = \sin x (1 + \cos x)$ in the interval $[0, \pi]$.		
Sol.	$f'(x) = \sin x(-\sin x) + (1 + \cos x)\cos x = \cos^2 x - \sin^2 x + \cos x$ $\text{So, } f'(x) = 2\cos^2 x + \cos x - 1 = (\cos x + 1)(2\cos x - 1) = 0$ $\text{Thus, critical points are } x = \pi, \frac{\pi}{3} \in [0, \pi]$ $\text{Now, } f(0) = 0, f\left(\frac{\pi}{3}\right) = \frac{3\sqrt{3}}{4} \text{ and } f(\pi) = 0$ $\text{Therefore, Sum of Maximum and minimum value of } f\left(\frac{\pi}{3}\right) = \frac{3\sqrt{3}}{4}$	I II III IV	1 $\frac{1}{2}$ $\frac{1}{2}$ 1
29.	Solve the following Linear Programming Problem graphically : Minimize $Z = 4x + y$ subject to $x + y \geq 3$ $x + 2y \geq 4$ $x, y \geq 0.$		

Sol.	<table data-bbox="477 596 1075 764"><tr><th>Corner point</th><th>Value of $Z = 4x + y$</th></tr><tr><td>A (0, 3)</td><td>3</td></tr><tr><td>B (2, 1)</td><td>9</td></tr><tr><td>C (4, 0)</td><td>16</td></tr></table> Because the feasible region is unbounded, $Z = 3$ might not be the absolute minimum. On plotting, $4x + y < 3$, we observe the region $4x + y < 3$ lies entirely below this dashed line, so there is no overlap. Since there are no common points, the minimum value is confirmed. Minimum value of Z is 3 at $x = 0$ & $y = 3$.	Corner point	Value of $Z = 4x + y$	A (0, 3)	3	B (2, 1)	9	C (4, 0)	16	1 For correct graph & shading 1 $\frac{1}{2}$ $\frac{1}{2}$
Corner point	Value of $Z = 4x + y$									
A (0, 3)	3									
B (2, 1)	9									
C (4, 0)	16									
30. (a)	Find the equation of a line passing through the point $(1, -1, 2)$ and parallel to x-axis. Also, find the shortest distance between this line and the line $\vec{r} = 2\hat{i} + \hat{j} - \hat{k} + \mu(3\hat{i} - 5\hat{j} + 2\hat{k})$.									
Sol.	Required Eq. of line: $\vec{r} = (\hat{i} - \hat{j} + 2\hat{k}) + \lambda(\hat{i})$ Now, $\vec{a_1} = \hat{i} - \hat{j} + 2\hat{k}$, $\vec{b_1} = \hat{i}$, $\vec{a_2} = 2\hat{i} + \hat{j} - \hat{k}$, $\vec{b_2} = 3\hat{i} - 5\hat{j} + 2\hat{k}$ So, $\vec{a_2} - \vec{a_1} = \hat{i} + 2\hat{j} - 3\hat{k}$, $\vec{b_1} \times \vec{b_2} = -2\hat{j} - 5\hat{k}$, $\vec{b_1} \times \vec{b_2} = \sqrt{29}$ Thus, Shortest distance = $\left \frac{-4+15}{\sqrt{29}} \right = \frac{11}{\sqrt{29}}$	I 1 II $1\frac{1}{2}$ III $\frac{1}{2}$								
OR										

30. (b)	Find the equations of the lines AC and BD, if coordinates of points A, B, C and D respectively, are (3, -4, 2), (-1, -2, 0), (4, 1, -1) and (4, 0, 5). Show that the lines AC and BD are perpendicular to each other.		
Sol.	Required eq. of line AC: $\frac{x-3}{1} = \frac{y+4}{5} = \frac{z-2}{-3}$ OR $\frac{x-4}{1} = \frac{y-1}{5} = \frac{z+1}{-3}$	I	1
	Required eq. of line BD: $\frac{x+1}{5} = \frac{y+2}{2} = \frac{z}{5}$ OR $\frac{x-4}{5} = \frac{y}{2} = \frac{z-5}{5}$	II	1
	Since, $1 \times 5 + 5 \times 2 + (-3) \times 5 = 5 + 10 - 15 = 0$		
	Therefore, the lines AC and BD are perpendicular to each other.	III	1
31. (a)	If R is a relation on set of natural numbers N such that $R = \{(x, y) : x, y \in N, x + 2y = 25\}$, then find the Domain and Range of the relation R. Also, determine if it is an equivalence relation.		
Sol.	As, $R = \{(23,1), (21,2), (19,3), (17,4), (15,5), (13,6), (11,7), (9,8), (7,9), (5,10), (3,11), (1,12)\}$	I	1
	Domain of relation R = {23, 21, 19, 17, 15, 13, 11, 9, 7, 5, 3, 1}	II	$\frac{1}{2}$
	Range of relation R = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12}	III	$\frac{1}{2}$
	Since, $1 \in N$, but $(1,1) \notin R$, So R is not Reflexive. Therefore, R is not an equivalence relation.	IV	1
OR			
31. (b)	Determine whether the function $f : \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = 2x^3 - 7$, $\forall x \in \mathbb{R}$ (Real numbers) is bijective or not.		
Sol. :	Let $f(a) = f(b)$, for some $a, b \in \mathbb{R} \Rightarrow 2a^3 - 7 = 2b^3 - 7$ $\Rightarrow a^3 = b^3 \Rightarrow a = b$, Thus, f is one-one function.	I	1
	Now, Let $y = f(x) = 2x^3 - 7 \Rightarrow x = \left(\frac{y+7}{2}\right)^{\frac{1}{3}}$	II	$\frac{1}{2}$

	For any real number y, the expression $\left(\frac{y+7}{2}\right)^{\frac{1}{3}}$ is a real number. Therefore, Range = $\mathbb{R}$ = Co-domain, so f is onto function. Since f is both one-one and onto, so it is a bijective function.	III	1
	SECTION D Q. Numbers 32 to 35 are long answer questions of 5 marks each.	IV	$\frac{1}{2}$
32.	Evaluate : $\int_0^{\pi/2} \frac{\sin^2 x}{1 + \sin x \cos x} dx$		
Sol.	Let $I = \int_0^{\frac{\pi}{2}} \frac{\sin^2 x}{1 + \sin x \cos x} dx = \int_0^{\frac{\pi}{2}} \frac{\cos^2 x}{1 + \sin x \cos x} dx$ $2I = \int_0^{\frac{\pi}{2}} \frac{1}{1 + \sin x \cos x} dx$ $I = \frac{1}{2} \int_0^{\frac{\pi}{2}} \frac{\sec^2 x}{1 + \tan x + \tan^2 x} dx$ Put $\tan x = p \Rightarrow \sec^2 x dx = dp$ $I = \frac{1}{2} \int_0^{\infty} \frac{1}{p^2 + p + 1} dp$ $I = \frac{1}{2} \int_0^{\infty} \frac{1}{\left(p + \frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2} dp = \left[\frac{1}{\sqrt{3}} \tan^{-1} \left(\frac{2p + 1}{\sqrt{3}} \right) \right]_0^{\infty}$ $I = \frac{1}{\sqrt{3}} \left(\frac{\pi}{3} \right) = \frac{\pi}{3\sqrt{3}}$	I II III IV V VI	1 1 $\frac{1}{2}$ 1 1 $\frac{1}{2}$

33. (a)	Let $\vec{\alpha}$, $\vec{\beta}$, $\vec{\gamma}$ be three non-zero vectors, such that $\vec{\alpha} \times \vec{\beta} = \vec{\gamma}$ and $\vec{\beta} \times \vec{\gamma} = \vec{\alpha}$. Show that α, β, γ are mutually perpendicular vectors such that $\vec{\beta} = 1$ and $\vec{\alpha} = \vec{\gamma}$. Find projection of vector $\vec{\alpha}$ on $\vec{\beta}$. Give reasons to support your answer.		
Sol.	As, $\vec{\alpha} \times \vec{\beta} = \vec{\gamma} \Rightarrow \vec{\gamma} \perp \vec{\alpha}$ and $\vec{\gamma} \perp \vec{\beta}$ Similarly, $\vec{\beta} \times \vec{\gamma} = \vec{\alpha} \Rightarrow \vec{\alpha} \perp \vec{\gamma}$ and $\vec{\alpha} \perp \vec{\beta}$ Thus, $\vec{\alpha}, \vec{\beta}$ and $\vec{\gamma}$ are mutually perpendicular vectors. Now, $\vec{\alpha} \times \vec{\beta} = \vec{\gamma} \Rightarrow \vec{\alpha} \vec{\beta} = \vec{\gamma}$ and $\vec{\beta} \times \vec{\gamma} = \vec{\alpha} \Rightarrow \vec{\beta} \vec{\gamma} = \vec{\alpha}$ Thus, $\vec{\beta} \vec{\alpha} \vec{\beta} = \vec{\alpha} \Rightarrow \vec{\beta} = 1$ (since, $\vec{\alpha} \neq 0$) On putting $\vec{\beta} = 1$ in the $\vec{\beta} \vec{\gamma} = \vec{\alpha}$, we get $\vec{\gamma} = \vec{\alpha}$ Projection of $\vec{\alpha}$ on $\vec{\beta} = 0$, as $\vec{\alpha} \perp \vec{\beta}$.	I II III IV V VI	1 1 1 1 $\frac{1}{2}$ $\frac{1}{2}$
OR			
33. (b)	If points A(3, -1, 2), B(6, -3, 6), C(4, -3, 1) and D(1, -1, -3) are vertices of a quadrilateral ABCD, write the position vectors of A, B, C and D and show that ABCD represents a parallelogram. Also, find the area of the parallelogram ABCD.		
Sol.	Position vector of A = $3\hat{i} - \hat{j} + 2\hat{k}$, Position vector of B = $6\hat{i} - 3\hat{j} + 6\hat{k}$ Position vector of C = $4\hat{i} - 3\hat{j} + \hat{k}$, Position vector of D = $\hat{i} - \hat{j} - 3\hat{k}$ Now, $\overrightarrow{AB} = 3\hat{i} - 2\hat{j} + 4\hat{k}$, $\overrightarrow{CD} = -3\hat{i} + 2\hat{j} - 4\hat{k} = -\overrightarrow{AB}$ Also, $\overrightarrow{CD} = \overrightarrow{AB}$ As, AB and CD are parallel and equal so ABCD represents a parallelogram. Since, $\overrightarrow{AB} = 3\hat{i} - 2\hat{j} + 4\hat{k}$, $\overrightarrow{BC} = -2\hat{i} - 5\hat{k}$	I II III IV	$\frac{1}{2}$ $\frac{1}{2}$ 1 1

	$\overrightarrow{AB} \times \overrightarrow{BC} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & -2 & 4 \\ -2 & 0 & -5 \end{vmatrix} = 10\hat{i} + 7\hat{j} - 4\hat{k}$	V	1
	Area of Parallelogram = $\sqrt{100 + 49 + 16} = \sqrt{165}$	VI	1
34.	Solve the differential equation $(x + y) dy + (x - y) dx = 0$, given that $y(1) = 1$.		
Sol.	Given differential equation can be written as, $\frac{dy}{dx} = \frac{y-x}{y+x} = \frac{\frac{y}{x}-1}{\frac{y}{x}+1}$	I	1
	Put $y = vx \Rightarrow \frac{dy}{dx} = v + x \frac{dv}{dx}$	II	1
	Thus, $v + x \frac{dv}{dx} = \frac{v-1}{v+1} \Rightarrow x \frac{dv}{dx} = \frac{-v^2-1}{v+1}$		
	$\Rightarrow \frac{v+1}{v^2+1} dv = -\frac{1}{x} dx$	III	1
	$\Rightarrow \frac{1}{2} \log(v^2 + 1) + \tan^{-1} v = -\log x + c$	IV	1
	$\Rightarrow \frac{1}{2} \log(y^2 + x^2) + \tan^{-1} \frac{y}{x} = c$	V	$\frac{1}{2}$
	Now, on putting $x = 1, y = 1$, we get $\frac{1}{2} \log(2) + \frac{\pi}{4} = c$		
	Therefore, $\frac{1}{2} \log(y^2 + x^2) + \tan^{-1} \frac{y}{x} = \frac{1}{2} \log(2) + \frac{\pi}{4}$	VI	$\frac{1}{2}$
35. (a)	Using integration, find the area bounded by the curve $y = x^2$ and the line $y = 2$.		
Sol.	 Required Area = $2 \int_0^2 x dy = 2 \int_0^2 \sqrt{y} dy$ $= 2 \left(\frac{y^{\frac{3}{2}}}{\frac{3}{2}} \right)_0^2$ $= \frac{4}{3} (2\sqrt{2}) = \frac{8\sqrt{2}}{3}$	I II III IV	1 (For correct graph) 2 1 1

	(i) If the building constructed was found to be strong, then what is the probability that the construction contract was given to the company X ? 2 (ii) If a part of the newly constructed building falls off, then what is the probability that it was due to the selection of company Y or Z ? 2		
Sol.	(i) $P(\text{strong construction quality}) = \frac{1}{3} \times \frac{80}{100} + \frac{2}{9} \times \frac{60}{100} + \frac{4}{9} \times \frac{70}{100} = \frac{640}{900}$ So, $P\left(\frac{\text{Construction Contract to X}}{\text{strong construction quality}}\right) = \frac{\frac{240}{900}}{\frac{640}{900}} = \frac{3}{8}$ (ii) $P(\text{Defective construction quality}) = \frac{1}{3} \times \frac{20}{100} + \frac{2}{9} \times \frac{40}{100} + \frac{4}{9} \times \frac{30}{100} = \frac{260}{900}$ So, $P\left(\frac{\text{Construction Contract to Y or Z}}{\text{strong construction quality}}\right) = 1 - \frac{\frac{60}{900}}{\frac{260}{900}} = \frac{10}{13}$	I II I II	1 1 1 1
38.	In a school, the swimming pool is shaped as a cuboid, and the breadth of the pool is represented by line $\frac{-x+2}{-5} = y = z - 3$. Two students A and B are swimming along the length of the pool. Based on the above information, answer the following questions : (i) If the path of student A is represented by line $\frac{x+5}{1} = \frac{y+3}{4} = \frac{z-6}{-3p}$, find the value of p. 1 (ii) Write the vector equation of the path of student B swimming parallel to the path of student A, if at a certain instant he passes through the point with coordinates (2, 4, -1). 1 (iii) (a) Find the foot of the perpendicular drawn from (2, 4, -1) to the path represented by student A. 2 OR (iii) (b) If a bird flies across the top of the swimming pool with its path represented by $\frac{x+4}{2} = \frac{y+3}{8} = \frac{z-5}{-18}$, then find the shortest distance between its path and the path of student A. 2		
Sol.	(i) $5 \times 1 + 1 \times 4 + 1 \times (-3p) = 0 \Rightarrow p = 3$ (ii) Vector equation of student B's path: $\vec{r} = (2\hat{i} + 4\hat{j} - \hat{k}) + \lambda(\hat{i} + 4\hat{j} - 9\hat{k})$ (iii) (a) Let the point be $Q(2, 4, -1)$ Let $P(\lambda - 5, 4\lambda - 3, -9\lambda + 6)$ be the foot of the perpendicular So, drs of PQ = $\langle \lambda - 7, 4\lambda - 7, -9\lambda + 7 \rangle$	I II I II	1 1 $\frac{1}{2}$ $\frac{1}{2}$

	Since PQ will be perpendicular to path of student A, so $\lambda - 7 + 16\lambda - 28 + 81\lambda - 63 = 0 \Rightarrow 98\lambda = 98 \Rightarrow \lambda = 1$ Thus, Required foot of the perpendicular from Q to path of A is $(-4, 1, -3)$.	III	$\frac{1}{2}$
	IV	$\frac{1}{2}$	
	OR		
	(iii) (b) As, drs of Bird path and drs of student A's path are proportional So, both paths (line) are parallel. Here, $\vec{a}_1 = -5\hat{i} - 3\hat{j} + 6\hat{k}, \vec{a}_2 = -4\hat{i} - 3\hat{j} + 5\hat{k}, \vec{b} = \hat{i} + 4\hat{j} - 9\hat{k}$ Now, $(\vec{a}_2 - \vec{a}_1) \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 0 & -1 \\ 1 & 4 & -9 \end{vmatrix} = 4\hat{i} + 8\hat{j} + 4\hat{k}$ Thus, required shortest distance = $\frac{\sqrt{96}}{\sqrt{98}}$ OR $\frac{4\sqrt{3}}{7}$	I	$\frac{1}{2}$
		II	1
		III	$\frac{1}{2}$